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Approximating scheduling for multimedia applications under overload conditions

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Abstract

With the increased demands in multimedia applications, the need to provide better system support is greater than ever. Multimedia applications have an added dimension of time in their execution which results in stringent timing requirements. These timing requirements are usually "soft" constraints, that is, they are potentially relaxable human preference constraints. In this paper, we investigate an approximating scheduling algorithm that attempts to derive a "good" schedule for multimedia processes even under the overload condition. A model is presented which is able to quantify the trade-off between conflicting goals in a multimedia application. Experiments are conducted to test the performance of the approximating scheduling algorithm. Results indicate that our proposed algorithm is able to adjust dynamically to transient overload situation without too much degradation in performance.

Keywords: Approximating scheduling; Predictable overload management; Real-time multimedia

1. Introduction

Multimedia applications place different demands on computer systems with the added dimension of time in their execution. For instance, the playback of a

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video sequence has to follow a pre-established frame rate of display to achieve an optimal presentation. Adhering to the timing constraint in frame rate is essential so that viewers do not experience too much jitters or unnatural 'jerkiness' in the display. Such constraints imposed on the execution of the application are "soft" constraints where there are penalties incurred if the deadlines are missed but the consequences of missed deadlines are non-critical. We term such systems as soft real-time systems. Many researchers have recognized the need for real-time support for multimedia applications. While many have developed communication protocols [6] and platforms [20] to support real-time transmission of data, scheduling the execution at the end-host computer has not received similar attention. Multimedia applications not only require large amounts of CPU time (to process complex video/audio images) but also demand that the CPU be allocated at pre-determined intervals (following the frame rate). As such, the scheduling mechanism in conventional general-purpose operating systems like UNIX, which emphasizes on fairness of distribution of CPU time (time-sharing) amongst all processes and not timeliness of delivery, cannot be used.

Yet, if we naively apply the techniques used in hard real-time systems (where missing a deadline is considered fatal) to schedule multimedia applications, the results obtained are usually not desirable. This is because while it may be possible to determine a priori the resource requirements of a multimedia application, such a priori determination results in an overly conservative schedule that does not take into consideration the characteristics and demands of multimedia applications. Multimedia applications typically exhibit the following characteristics:

Variable rate of execution: While most multimedia applications execute periodically, the execution rate does not need to strictly follow a fixed rate. For example, a video-on-demand application may have an optimal rate of 20 frames per second (fps). But if the system is overloaded, the execution may, for short spells of time, degrade to 10 fps without significant loss of quality.

Non-static computation time: The execution time for a task may fluctuate depending on the data it is working on. Such cases happen due to the dynamic nature of multimedia data. In MPEG video data, frames can be encoded as either I-frames (intra-coded frame), P-frames (predictive-coded frame) or B-frames (bi-directionally predictive-coded frame). I-frames are coded without any reference to other images. P- and B-frames require information of the previous and/or future I/P-frames. As a result, decoding I-frames require much more computation time as compared to decoding P- or B-frames. This results in non-static computation time.

Incomplete execution: Quite often, the quality of a video sequence is gradually improved through many phases of refinement. If there is time to spare, a frame can undergo several iterations to produce a high quality output. But if there is insufficient time, then a less-than-perfect output is achieved. This

compromise in execution will produce a video sequence with a mix of high and low quality frames, something certainly more desirable than expecting high quality frames all the time, causing the task to miss all the deadlines in the process.

Relaxed deadlines: If a multimedia task completes execution after its deadline, the outcome should not be abandoned, even though the *value* obtained may not be as high as if the task is completed by the deadline. This is because most multimedia tasks do have a level of tolerance due to the variations in the level of human sensory perception. For example, in the case of an audio and video playback application, the synchronization points of the two streams are loosely bounded up to approximately 250 ms [8]. Under such circumstances, even if one of the media streams is late at output, the jitter may not be easily detected by the user.

In this paper, we first propose a model that depicts these characteristics of multimedia applications. An approximating scheduling algorithm is then presented that can be used to schedule multimedia tasks effectively on a single processor.

2. Related work

Much work has been done in the area of real-time scheduling algorithms. The Earliest Deadline (ED) algorithm [15] is an optimal dynamic scheduling algorithm that is able to schedule all tasks correctly provided the system is not overloaded. However, if the system was to be temporarily overloaded, the ED algorithm will fail miserably.

Researchers have adopted different approaches to try to solve this problem. Tia et al. [21] model the varying computation time as a probability density function and then use existing scheduling algorithms (e.g. Rate Monotonic [15] with Sporadic Server [19]) to provide statistical guarantees on the execution. Mok and Chen [17] model the computation time instead with a fixed repeating sequence and establish a sufficient condition for optimal execution if the sequence is *accumulative monotonic* [2]. Besides trying to model the execution time, others have concentrated on coping with overload conditions instead, and thus indirectly address the problem of variable execution time.

Many heuristics have been proposed for best-effort delivery under overload conditions [7,10,12]. They usually involve using an optimal scheduling algorithm under normal conditions, and then switching to a best-effort algorithm

[2] [17] Given a task $T = ((c_1, c_2, \ldots, c_n), p)$, where c_i denotes the computation time and p denotes the period of the task, and c_1 is the largest. $\forall i, 1 \leqslant i \leqslant n, \forall k, 1 \leqslant k \leqslant n - i$.
$\sum_{j=1}^{k+1} c_j \geqslant \sum_{j=i}^{k+i} c_j$.

when the demand exceeds a certain threshold. A significant breakthrough in the study of overload scheduling is the proof by Baruah et al. [2] that no online algorithm is able to guarantee a value of greater than $\frac{1}{4}$th the value obtained by a clairvoyant [3] scheduler.

On the other hand, the approach taken by multimedia researchers is empirical and involves observing the performance of a particular multimedia application. In Fall et al. [4], an existing video-conferencing application is examined and modifications are proposed to its video segment to support CPU load adaptation. The mechanism involves a *Load Agent* which monitors the Interframe Display Time (IDT) and induces the application to discard frames if the variance of the IDT increases over a threshold. Jeffay [9] implemented a programming model based on Rate-based Execution (RBE). The basis is a resource-allocation model which guarantees that an application will progress at least at its specified rate. When resources are scarce, a negotiation will take place to reduce the rate of progress. In similar fashion, the RT-Mach research for multimedia support [13] utilizes a reservation system for processor capacity. Under overload condition, the application can choose to lower the rate of execution or reduce the quantum of processor usage at every period. Experiments conducted by Gerber and Ghavai [5] on a video-playback application suggest that simply decreasing the desired frame-rate does not always guarantee a better quality result. These observations point to the fact that some systematic way of managing overload is necessary to ensure execution is maintained at the best possible level. In our work, the user is asked to specify a compromise criterion. Our scheduler will then regulate the overload condition based on the specified criterion. The specification of the compromise criterion is based on the concepts of mandatory and optional sub-tasks defined in the imprecise computation technique [14,3]. Every task is divided into two parts, a mandatory sub-task which must be executed and will produce an acceptable result as well as an optional sub-task which will serve to refine and improve the result. The optional sub-task is assumed to be monotonically increasing, implying that more time spent on execution will guarantee a better result. Thus, in overload condition, the optional sub-tasks are those that can be compromised to allow the mandatory sub-tasks to be completed. A point to note is that this compromise criterion is a fuzzy linguistic variable that allows scheduling decision to be made under vague constraints. Slany [18] examines the problem of scheduling under vague constraints and uncertain data. He uses a combination of fuzzy set based constraints and repair based heuristics to model such scheduling problems.

[3] knowing the parameters of future events.

3. Multimedia task model

In the section, we propose a model for representing multimedia tasks. This model can then be used to perform the scheduling of tasks. Our task model is hierarchical in nature. At the top, the task model consists of a few task sets. Each task set is simply a collection of several independent tasks, competing with each other for processing time. Each task is, in turn, a sequence of operations. This is akin to a computer system (task model) having a few executing multimedia applications (task sets) containing several media streams (tasks), and each stream executing its own subroutines (e.g. 3 operations, input → processing → output) (see Fig. 1). Each task, T_i, has a start time, a period and a corresponding deadline for each release of the task at each period. Formally,

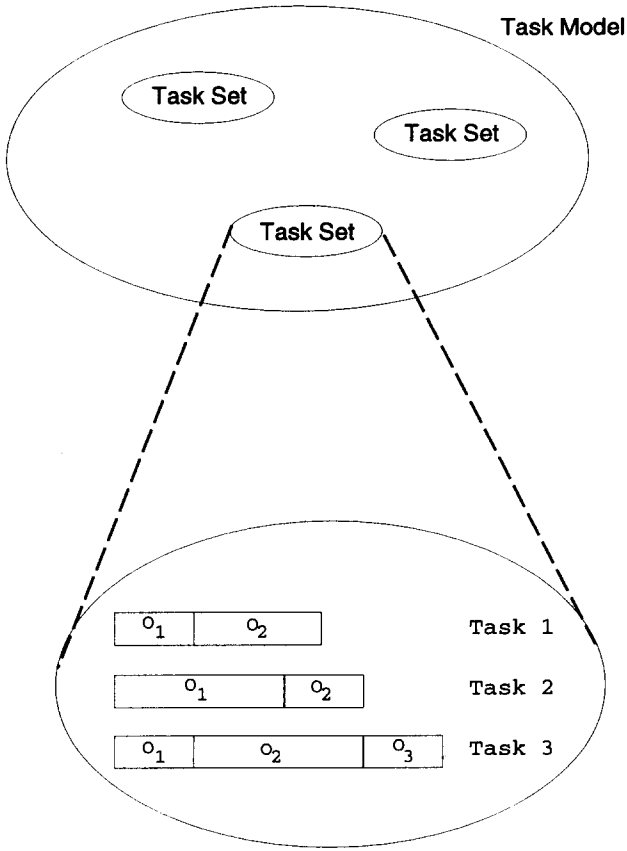

Fig. 1. The task model.

the task set is defined as $\tau = \{T_1, T_2, \ldots, T_n\}$ where n is the total number of tasks and $T_i = (O_i, r_i, p_i, d_i)$ where $O_i = [O_i^1, O_i^2, \ldots, O_i^m]$, m is $|O_i|$, r_i is the ready time or start time, p_i the period and d_i the relative deadline. Thus task T_i is released at times $r_i, r_i + p_i, r_i + 2p_i, \ldots$ and has deadlines at $r_i + d_i, r_i + p_i + d_i$, $r_i + 2p_i + d_i, \ldots$. The operation O_i^k is a 2-tuple $(oc_i^k, \text{Rate}_i^k)$, where oc_i^k represents the computation time of the operation and Rate_i^k is the *desired rate* at which the particular operation is to run under normal load condition. Rate_i^k is a linguistic variable [11] with the values of "compulsory", "frequent", "occasional" and "rare". The universe of discourse is the interval $[0, 1]$. The membership curves of the linguistic values are shown in Fig. 2. In addition, we also define c_i as the total computation time of task T_i, and $c_i = \sum_{j=1}^{m} oc_i^j$.

A point to note is that in a sequence of operations $O_i = [O_i^1, O_i^2, \ldots, O_i^m]$ in task T_i, the execution of operation O_i^k is not a pre-requisite for the execution of O_i^{k+1}. When scheduling T_i, the scheduling algorithm may, after the execution of O_i^{k-1}, discard O_i^k and immediately schedule O_i^{k+1}. In practical situations, the task T_i can be a video stream and the operation O_i^k is a dithering subroutine which improves the quality of the images. Under overload condition, we may want to sacrifice the quality of the image (by discarding O_i^k) in exchange for on-time delivery of the video stream. This trade-off between quality and time can be expressed using a set of rules. Assume *Load* denotes the system load at a particular instant of time, *Rate* is the user-specified desired rate for an operation O, and Z is the target rate for O. The set of trade-off rules are as follows.

Rule1	If Load = heavy, Rate = compulsory then Z = compulsory
Rule2	If Load = normal, Rate = compulsory then Z = compulsory
Rule3	If Load = light, Rate = compulsory then Z = compulsory
Rule4	If Load = heavy, Rate = frequent then Z = occasional
Rule5	If Load = normal, Rate = frequent then Z = frequent
Rule6	If Load = light, Rate = frequent then Z = frequent
Rule7	If Load = heavy, Rate = occasional then Z = rare
Rule8	If Load = normal, Rate = occasional then Z = occasional
Rule9	If Load = light, Rate = occasional then Z = occasional
Rule10	If Load = heavy, Rate = rare then Z = very rare
Rule11	If Load = normal, Rate = rare then Z = rare
Rule12	If Load = light, Rate = rare then Z = rare

To obtain the value of Z, we first compute the degree of match between our inputs (the actual system load at the particular instant of time, and the desired execution rate of the operation) and the antecedent of each if-then rule. The calculation of the degree of match is based on standard fuzzy intersection. For example, suppose the system load at a given instant is SL, the desired

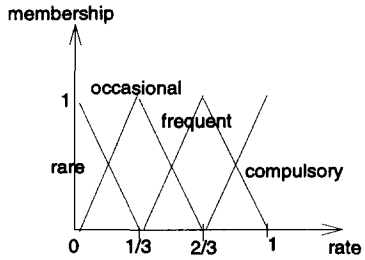

Fig. 2. The fuzzy concepts corresponding to the linguistic values of Rate_i^k.

execution rate for the operation is frequent (see Fig. 3), we see that Sl partially matches the antecedent of Rules 1 and 2. Hence, each rule's conclusion is truncated by the degree of match. Finally, we take the union of the truncated sets to arrive at a conclusion (see Fig. 3). This conclusion is a fuzzy set. To obtain a numerical value, we perform defuzzification of the conclusion using the center of maxima method [11]. The defuzzified value, denoted by f, is a numerical value between 0 and 1. We say f is the theoretical desired frequency of the operation. Suppose the value of f is $1/n$, then this implies that for every n number of operations, the user is satisfied with the quality obtained if only one out of every n is being executed. Note that by allowing the user to specify different desired frequency rates at the operation level, we give the user greater control

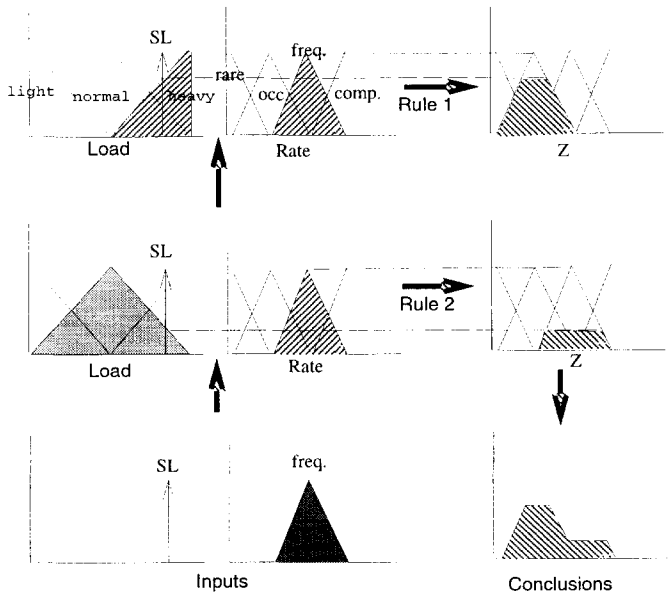

Fig. 3. The reasoning process.

over the handling of different video frame types. For example, we may define one operation to handle the keyframes (I-frames), another operation to handle the P-frames and a third operation to handle the B-frames. Since dropping an I-frame degrades the quality of the video much more as compared to dropping a P- or B-frame, we specify a higher frequency rate for the operation handling the I-frame, while the operations handling P- or B-frame are given lower frequency rate. With this, we exert a finer control over the handling of different video frame types thus allowing the quality of service be maintained to a satisfactory degree even under overload condition. The same argument goes for the handling of audio data. A higher frequency may be assigned to the operation handling audio samples. This can prevent too many of the audio samples from being dropped thus maintaining the desired sound quality.

4. Approximating scheduling algorithm

A two-levels scheduling scheme is proposed to adapt to overload conditions. Fig. 4 shows the organization of the scheduling scheme. The first level is a frequency filter (FF) agent which uses the f obtained from the previous section to decide whether a particular operation should be discarded or admitted into the system. If the operation is to be admitted, it is then sent to the second-level scheduler for further scheduling, else it is returned to the task to invoke the next operation.

Two strategies have been implemented to perform the filtering process.

Cumulative filtering: This algorithm maintains a small counter for each operation. The counters are initialized with a randomly generated number between 0 and 1. When an operation is invoked, f is added to the counter. If the value of the counter is more than or equal to 1, the operation passes through the filter; otherwise, the operation is discarded. On successful execution of the operation, the counter is decreased by 1. This algorithm runs in O(1) time.

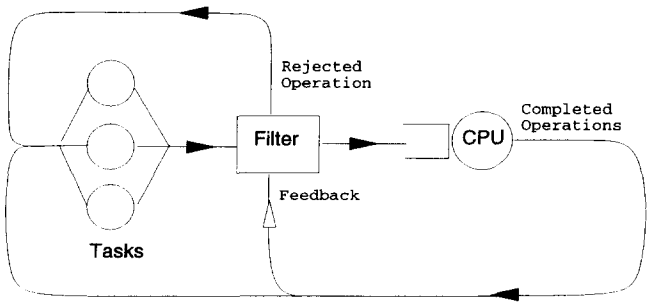

Fig. 4. Role of the frequency filter agent.

Probabilistic filtering: First, a random number generator is used to come up with a value between 0 and 1. Upon the arrival of an operation, f is compared with this random value. If f is equal or larger, the operation passes through; otherwise, it is discarded. The speed of this algorithm depends solely on the speed of the generator, which in this case, can be as simple as taking the nanosecond reading of the system clock, implying also a running time of O(1).

With the FF agent, we effectively prevent the less important operations (lower frequencies) from entering the second-level scheduler if the system load is already high, thus avoiding overload condition. As a result, many existing scheduling algorithms that have been proven to work well under light-normal conditions can be utilized at this second-level scheduler. Among the more well-known scheduling algorithms are:

1. *Earliest Deadline First (EDF):* Tasks waiting for the CPU are sorted in ascending order of their deadlines. The task with the earliest deadline will be executed first. The EDF algorithm is optimal so long as the CPU utilization is less than 1 [15].

2. *Least Slack (LS):* This is also an optimal dynamic scheduling algorithm [16] for preemptive systems. It is based on the urgency of tasks whereby the more urgent tasks (tasks with the least slack time) will be scheduled first. Slack time is the "spare" time that a task can spend waiting for execution before it misses its deadline.

3. *Shortest Remaining Processing Time First (SRPT):* This algorithm basically assigns tasks with the shortest remaining processing time to be executed first. This is adapted from the *shortest processing time* algorithm used in job-shop scheduling to minimize average lateness [1]. In this algorithm, tasks which can complete the job sooner are given higher priority and tasks with extremely long execution times are usually sacrificed.

4. *First Come First Served (FCFS):* This is the simplistic approach whereby a task that arrives first will be executed first.

Three sets of experiments are performed to see how well the proposed filtering strategies work in combination with these four well-known scheduling algorithms. Before we discuss the details of these experiments, let us first define the evaluation criteria for the goodness of the proposed strategies. Recall that f denotes the theoretical desired frequency of an operation. This theoretical desired frequency is derived based on the given system load at that particular instant of time and the user's specification of the desired rate as discussed in the previous section. However, in an actual implementation, this theoretical frequency usually differs from the actual frequency at which an operation is being invoked. We define the actual frequency (A) of an operation as the ratio of the number of times the operation is being executed to the total number of arrivals of the operation. Two measures are defined for evaluating the goodness of the proposed algorithm.

Operation variance: After every run, the individual variance of each of the operation within each task is computed by obtaining the square of the difference between the desired frequency (f) and the actual frequency (A) if the actual frequency is lower; and 0 if the actual frequency is equal or higher. Operation variance is then defined as the mean of all the individual variances. In other words,

$$\text{Individual variance} = \begin{cases} (f-A)^2 & (f > A), \\ 0 & (f \leqslant A), \end{cases}$$

$$\text{Operation variance} = \sum \frac{\text{individual frequency difference}}{\text{no. of runs} \times \text{no. of operations}}.$$

The rational for this measure is that so long as an operation runs above the theoretical desired frequency, there is no penalty involved because the quality level is what the user is willing to accept. Penalty is only incurred when $A < f$. Hence, by this definition, the larger the variance is, the greater is the amount of penalty. Therefore, this measure gives a good indication of the quality trade-off incurred by different scheduling algorithms.

Task variance: After every run, for each task, the individual task variance is computed as follows:

$$\text{Individual frequency difference} = \begin{cases} (f-A) & (f > A), \\ 0 & (f \leqslant A), \end{cases}$$

$$\text{Individual task variance} = \left(\sum \frac{\text{individual frequency difference}}{\text{no. of operations}} \right)^2,$$

$$\text{Task variance} = \sum \frac{\text{individual task variance}}{\text{no. of runs} \times \text{no. of tasks}}.$$

Table 1
Parameters for soft real-time tasks

Parameter	Value
Ready time of task	Exponential(20)
No. of operations/task	Uniform(2,5)
Compute time/operation	Exponential(5)
Overhead/operation	0.001
Period of task	Uniform(c_i,c_i*30)
Frequency	$\frac{\text{Random}(1,10)}{10}$

The task variance measure is the normalized aggregate of individual operation variance. It is used to determine the total amount of penalty incurred per task. Ideally, we would like to keep this measure as small as possible.

We performed the experiments on a Silicon Graphics Indy workstation running IRIX 5.3. A set of tasks is simulated with the parameter values as shown in Table 1. For each experiment, 50 runs are performed. In the first experiment, we test the effectiveness of combining cumulative filtering (CF) with the Earliest Deadline First algorithm (EDF-CF), the Least Slack algorithm (LS-CF), the First Come First Served algorithm (FCFS-CF) and the Shortest Remaining Processing Time algorithm (SRPT-CF). In the second experiment, we repeat the test using the probabilistic filtering (PF) technique with the four scheduling algorithms respectively: EDF-PF, LS-PF, FCFS-PF and SRPT-PF. Finally, we compare the best result of these two experiments with the performance of the scheduling algorithms without any filtering strategy.

The average results are presented below. In Figs. 5–8, the SRPT-CF and SRPT-PF algorithms are consistent in obtaining good results.

Next, we compare the SRPT-CF and SRPT-PF's performance with respect to the unfiltered algorithms (EDF, LS, FCFS, SRPT). From Figs. 9 and 10, we see that a suitable first-level filter is able to help obtain the best performance while a poorly designed one can lead to undesirable results.

5. Conclusion

In this paper, we have proposed an approach to handle scheduling of multimedia applications under variable and overload situations. This is because in

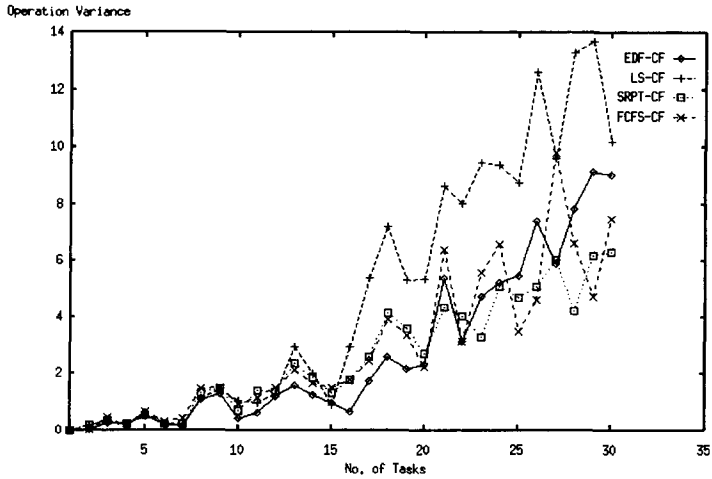

Fig. 5. Graph of operation variance under cumulative filtering.

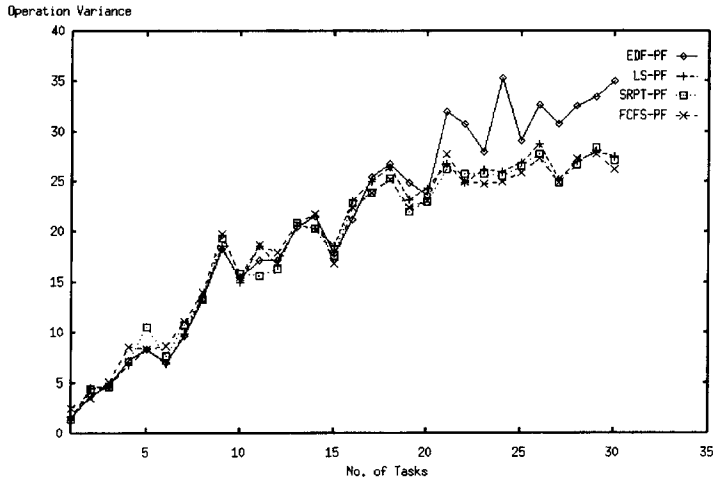

Fig. 6. Graph of operation variance under probabilistic filtering.

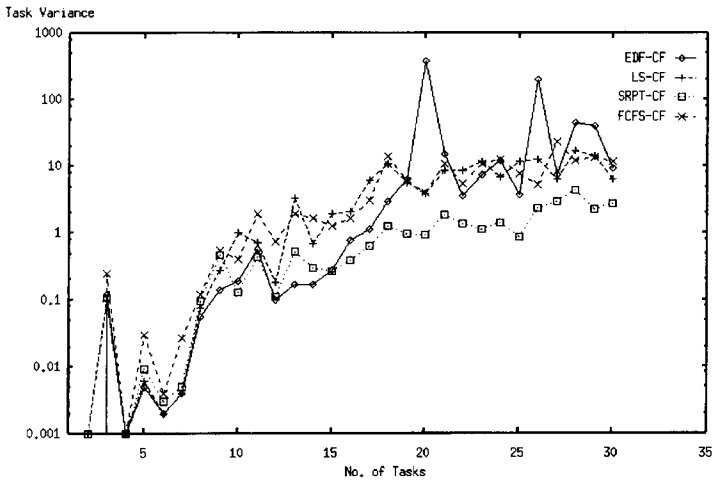

Fig. 7. Graph of task variance under cumulative filtering.

such situations, all the applications cannot be guaranteed to execute within their deadlines and hence, some form of degradation is necessary. Users are able to influence the schedule by specifying a frequency parameter associated with each operation of the task (or application). This parameter is a linguistic variable and it represents the *minimum desired rate* of the operation which the scheduling algorithm is expected to adhere to and hence achieve higher predictability in execution. A two-level scheduling strategy is proposed to incorporate

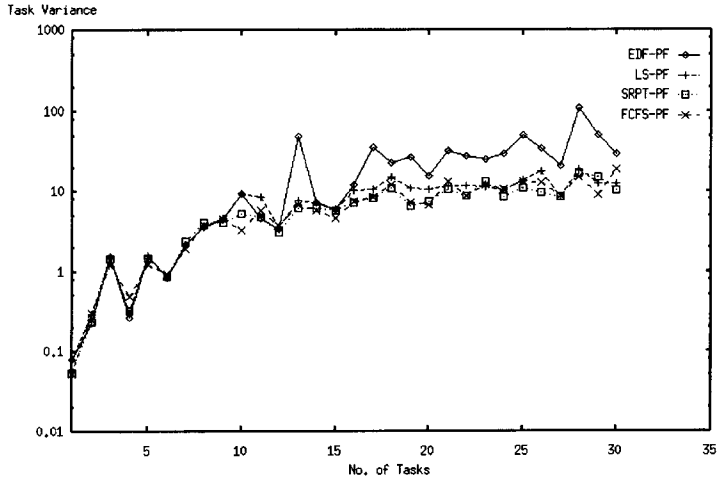

Fig. 8. Graph of task variance under probabilistic filtering.

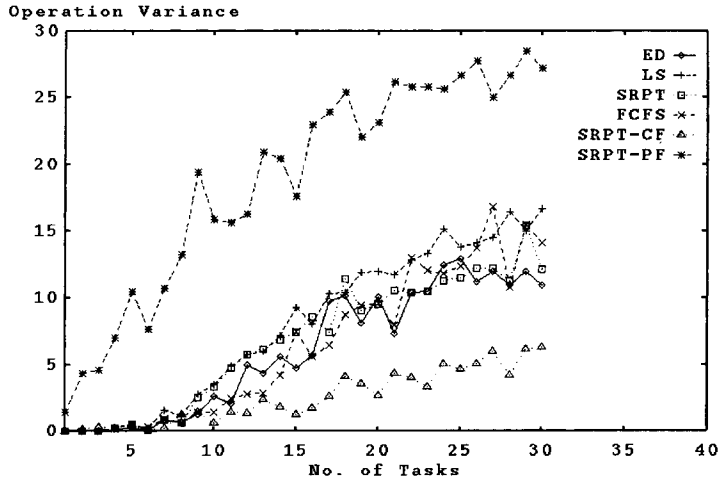

Fig. 9. Graph of operation variance.

the concept of minimum desired rate into the scheduling process. The simulation results indicate that the introduction of a simple frequency filtering agent, when used in conjunction with existing scheduling algorithms, can improve the schedule significantly under overload condition. Further work is in progress to analyze the impact of the filtering agent so as to achieve better and more stable results.

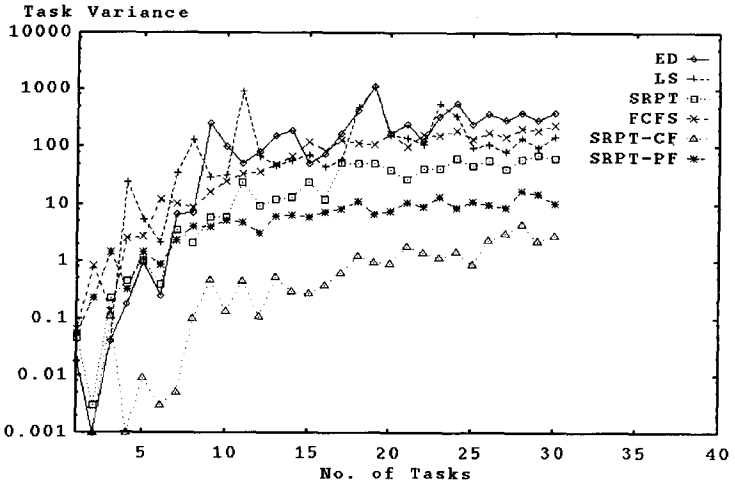

Fig. 10. Graph of task variance.

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